

Probabilistic Graphical Models

A Brief Overview of Trustworthy Machine Learning

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Lecture 28, April 29, 2020





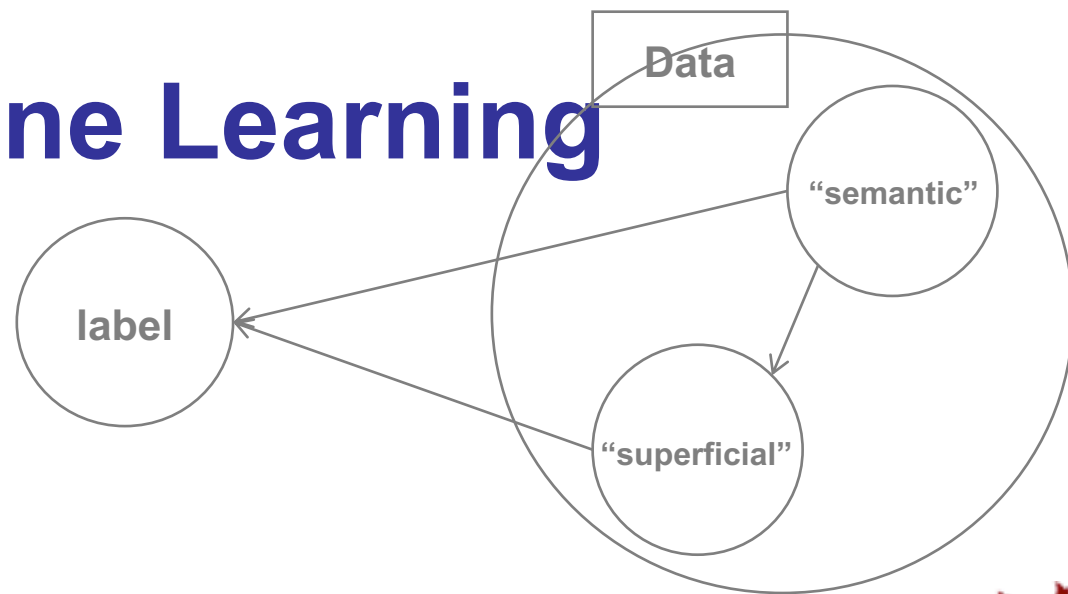
A Brief Overview of Trustworthy Machine Learning

- ❑ New Challenges of Modern Machine Learning
 - ❑ Empirical Observations
 - ❑ Trade-off between Accuracy and Robustness
- ❑ Cross-domain Robust Models
 - ❑ Generalization Analysis of Domain Adaptation
 - ❑ Method Overview – It's mostly about Invariance
 - ❑ Domain Generalization and Beyond
- ❑ Adversarial Robust Models
 - ❑ The Attack vs. Defense Arm Race Highlights
 - ❑ Adversarial Training and Its Recent Developments
 - ❑ Certified Robustness and Generalization Analysis





New Challenges of Modern Machine Learning

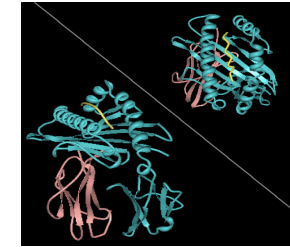




What if I told you...



- We can predict whether you use chopsticks from your genome.
 - HLA-A1 gene
 - (Vilhjálmsen and Nordborg, 2013)



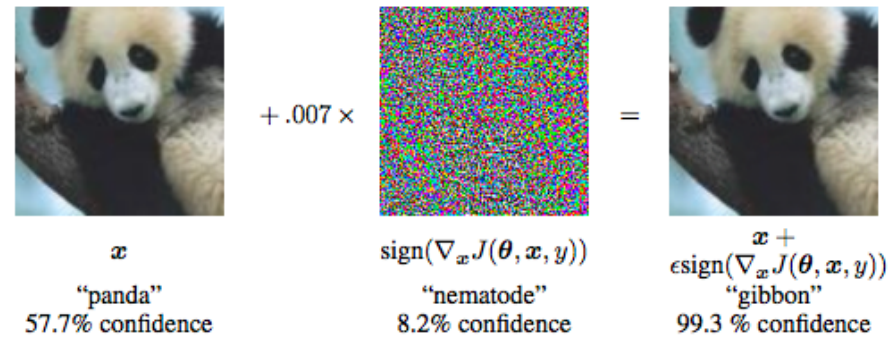
- We can predict whether you speak English or Welsh from your genome
 - (Weale et al 2002)
- Trustworthy statistical models research dates to decades ago...
 - E.g., population stratification in GWAS (Devlin, B. and Roeder, K. 1999)



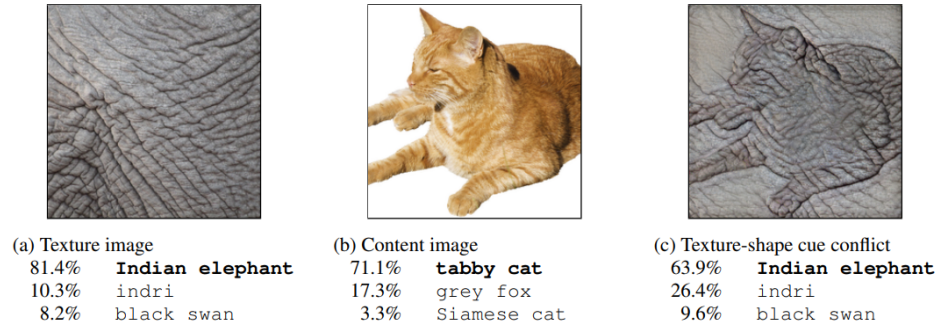


Behind the Glory of Deep Learning

- Adversarial example
 - (Szegedy et al 2013)



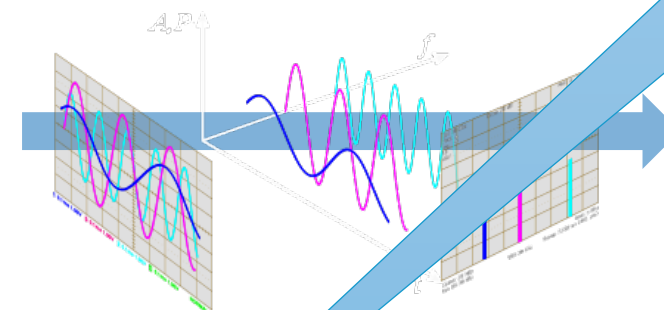
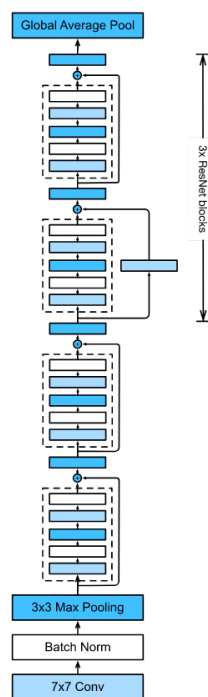
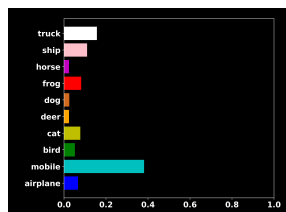
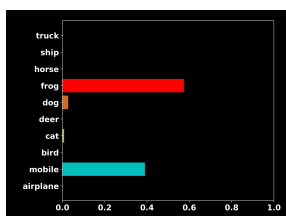
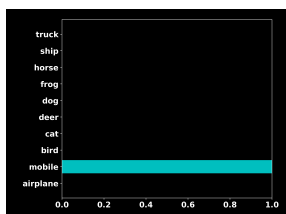
- CNN's tendency in superficial statistics
 - (Jo and Bengio 2017)
 - (Geirhos et al 2019)





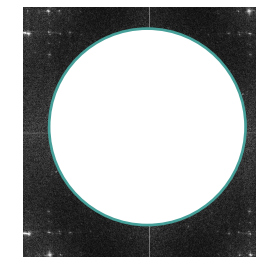
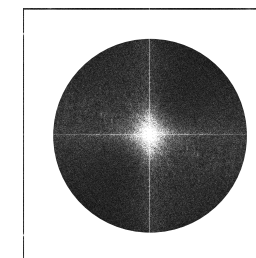
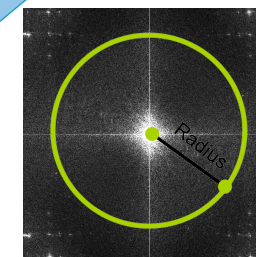
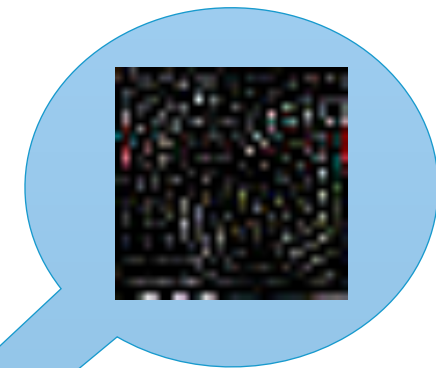
The Misalignment between CNN and Human

- CNN captures high-frequency information
 - (Wang et al, 2020)



Reconstruction

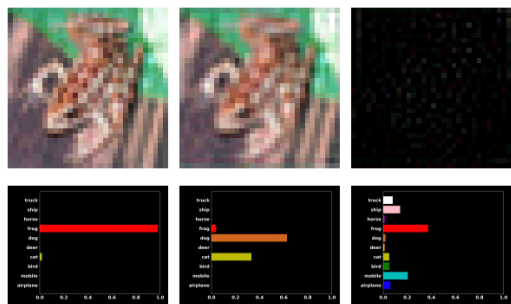
Reconstruction



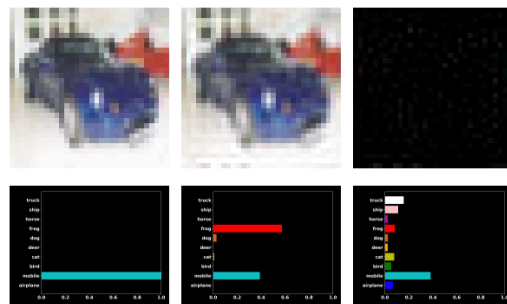


The Misalignment between CNN and Human

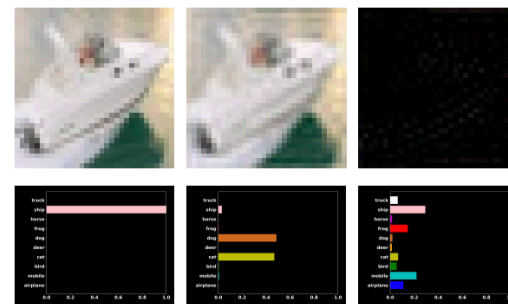
- CNN captures high-frequency information
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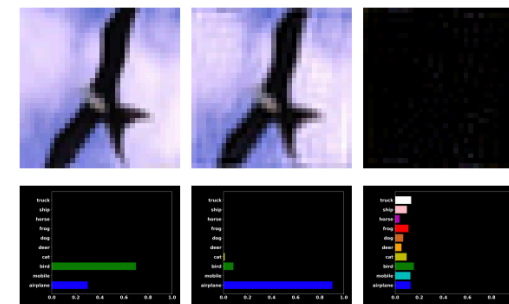
(a) A sample of frog



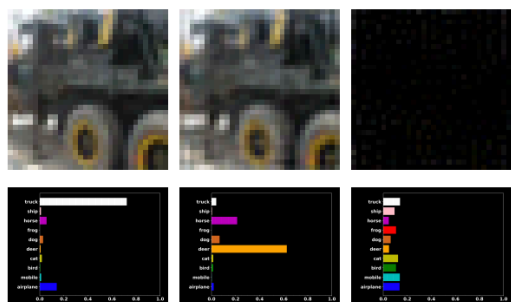
(b) A sample of mobile



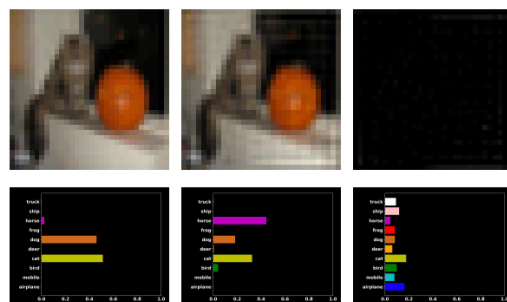
(c) A sample of ship



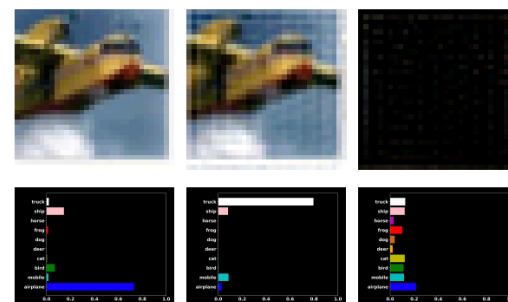
(d) A sample of bird



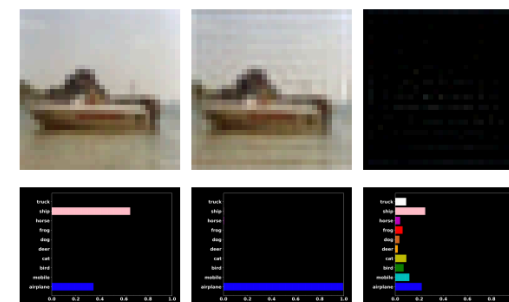
(e) A sample of truck



(f) A sample of cat



(g) A sample of airplane



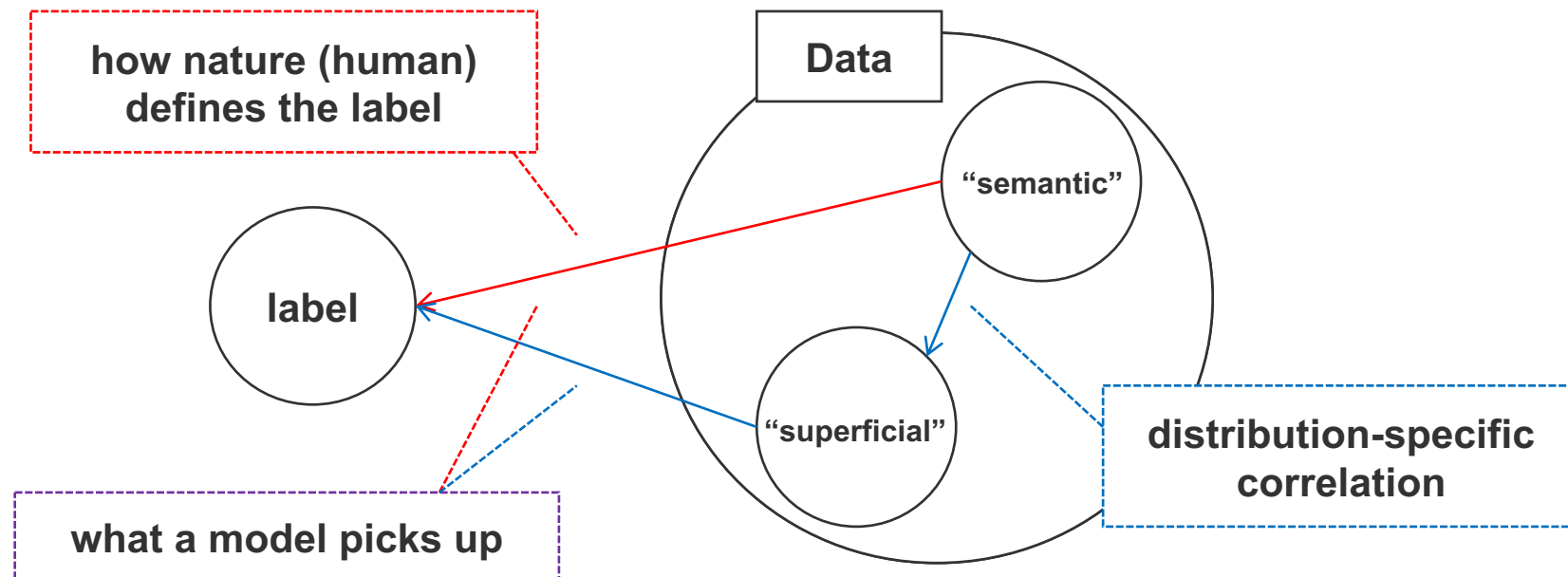
(h) A sample of ship





The New Challenge of Modern Machine Learning

- The misalignment between models and the nature/human
 - (Wang et al, 2020)



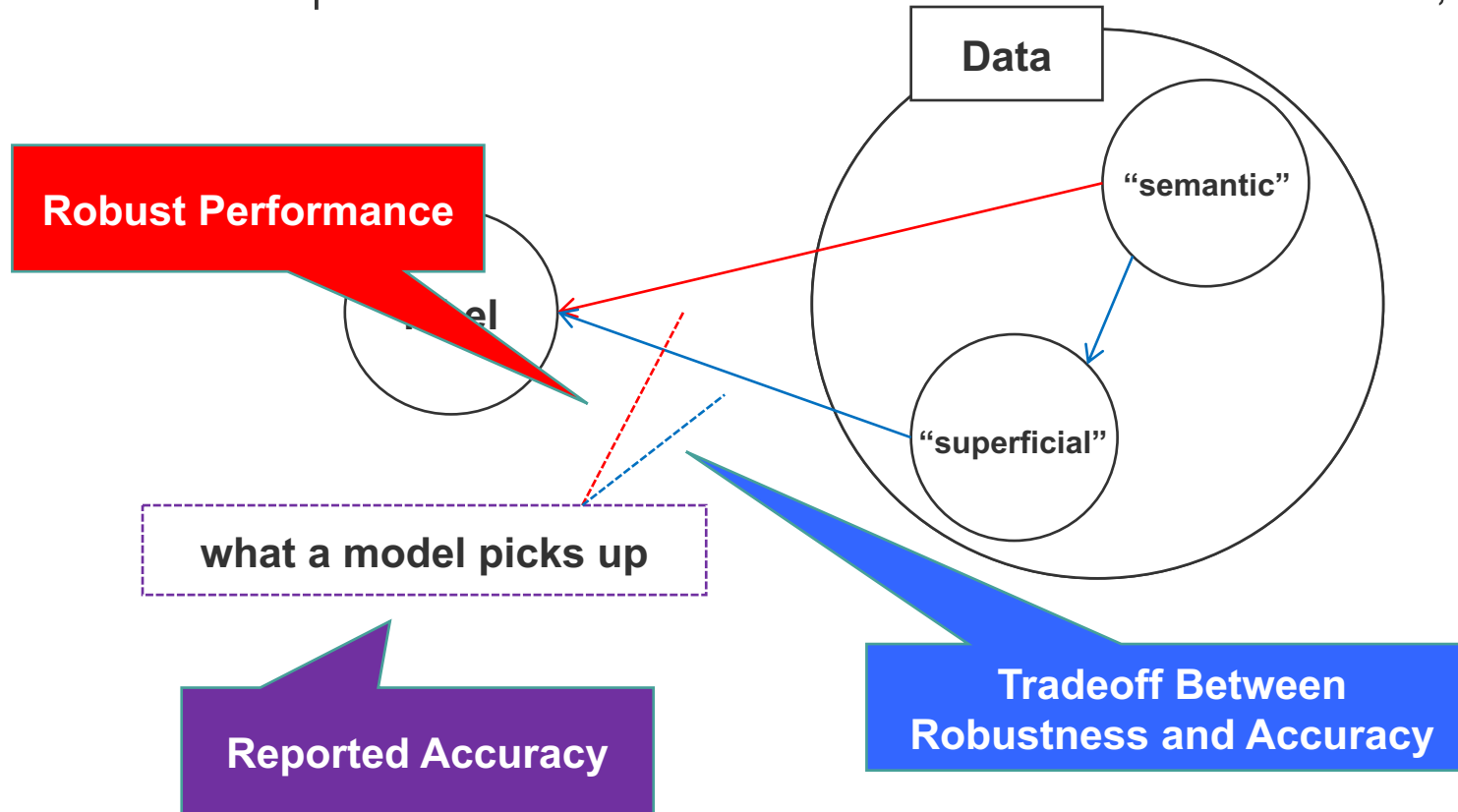
The central problem of today's lecture





The Tradeoff between Accuracy and Robustness

- It depends on how one defines “robustness”, but roughly



- Formal Discussions
 - Tsipras *et al* 2019
 - Zhang *et al* 2019
 - Yang *et al* 2019
 - Wang *et al* 2020





Why robustness is valued when we have accuracy

- What the current academy is good at





Why robustness is valued when we have accuracy

- ▣ What the world needs

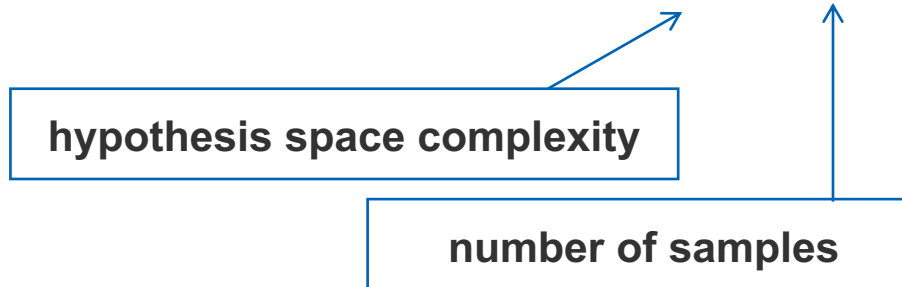




The Solution

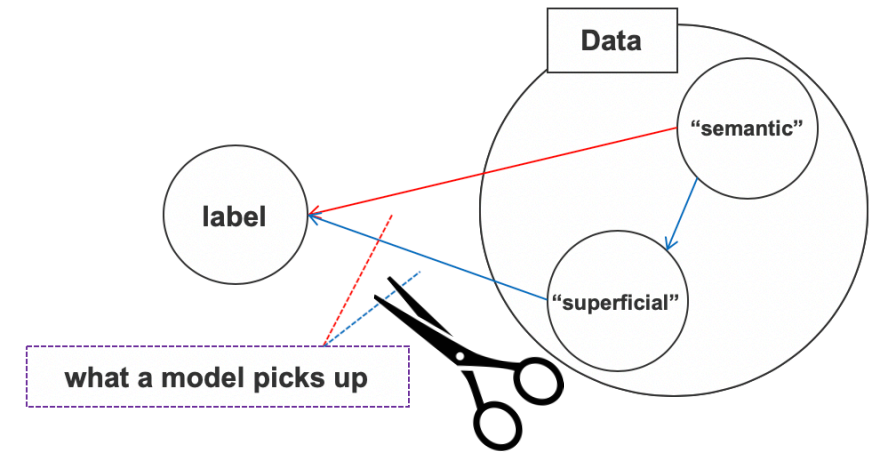
- To summarize it in one sentence
 - Machine learning is about generalization

$$R(h) \leq R_{\text{emp}}(h) + f(|H|, N, \delta)$$



- Cross-domain Robustness
 - Almost all about hypothesis space (*i.e.*, inductive bias, regularization)
- Adversarial Robustness
 - The dominant solution increases the number of samples

The central solution of today's lecture

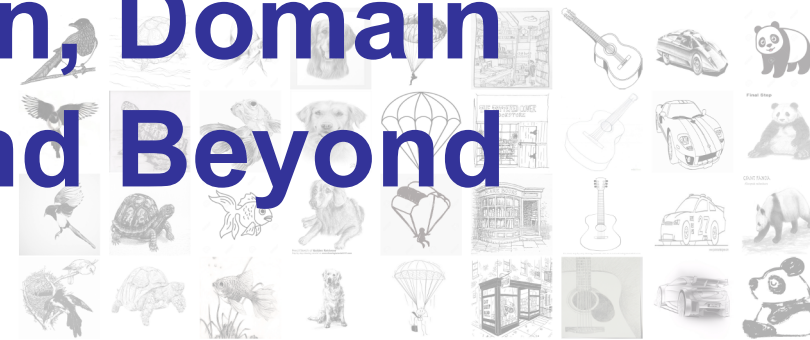




Cross-Domain Robustness: Domain Adaptation, Domain Generalization, and Beyond



ImageNet



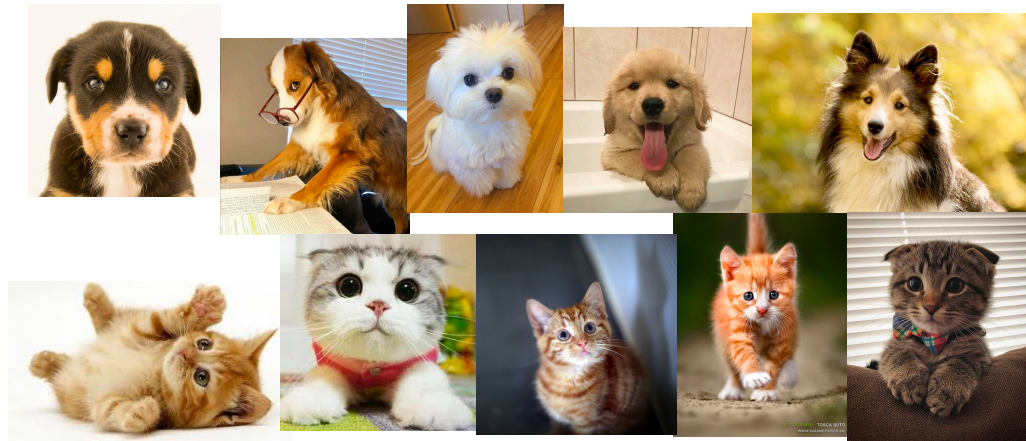
ImageNet-Sketch





Domain Adaptation

- ❑ Model is trained on one distribution/domain, but tested on a “similar but different” distribution/domain
 - ❑ Supervised domain adaptation
 - ❑ Some labelled samples in the test distribution are available during training
 - ❑ Unsupervised domain adaptation
 - ❑ Only unlabeled samples in the test distribution are available during training



During Training



During Testing





How is the generalization changed in UDA

- $\mathcal{H}$ -divergence: a measure of two distributions given a hypothesis class
 - $I(h)$: the set of hypotheses that are characteristic functions for the domain
 - $\mathcal{H}$ -divergence between the two distributions

$$d_{\mathcal{H}}(\mathcal{D}, \mathcal{D}') = 2 \sup_{h \in \mathcal{H}} |\Pr_{\mathcal{D}} [I(h)] - \Pr_{\mathcal{D}'} [I(h)]|$$

- Can be estimated from finite samples
 - U and U' are samples of size m :

$$d_{\mathcal{H}}(\mathcal{D}, \mathcal{D}') \leq \hat{d}_{\mathcal{H}}(\mathcal{U}, \mathcal{U}') + 4\sqrt{\frac{d \log(2m) + \log(\frac{2}{\delta})}{m}}$$

- Estimated from a domain classifier
 - For a symmetric hypothesis class both h and $1-h$ are in the hypothesis class

$$\hat{d}_{\mathcal{H}}(\mathcal{U}, \mathcal{U}') = 2 \left(1 - \min_{h \in \mathcal{H}} \left[\frac{1}{m} \sum_{\mathbf{x}: h(\mathbf{x})=0} I[\mathbf{x} \in \mathcal{U}] + \frac{1}{m} \sum_{\mathbf{x}: h(\mathbf{x})=1} I[\mathbf{x} \in \mathcal{U}'] \right] \right)$$





How is the generalization changed in UDA

- symmetric difference hypothesis space

$$g \in \mathcal{H} \Delta \mathcal{H} \iff g(\mathbf{x}) = h(\mathbf{x}) \oplus h'(\mathbf{x}) \text{ for some } h, h' \in \mathcal{H}$$

$$d_{\mathcal{H} \Delta \mathcal{H}}(\mathcal{D}_S, \mathcal{D}_T) = 2 \sup_{h, h' \in \mathcal{H}} |\Pr_{x \sim \mathcal{D}_S} [h(x) \neq h'(x)] - \Pr_{x \sim \mathcal{D}_T} [h(x) \neq h'(x)]|$$

- Generalization analysis
 - (Ben-David et al 2010)

A hypothesis space that is small enough so that the model does not differentiate source and target distribution

$$\epsilon_T(h) \leq \epsilon_S(h) + \frac{1}{2} \hat{d}_{\mathcal{H} \Delta \mathcal{H}}(\mathcal{U}_S, \mathcal{U}_T) + 4 \sqrt{\frac{2d \log(2m') + \log(\frac{2}{\delta})}{m'}} + \lambda$$

$$\lambda = \epsilon_S(h^*) + \epsilon_T(h^*)$$

$$h^* = \operatorname{argmin}_{h \in \mathcal{H}} \epsilon_S(h) + \epsilon_T(h)$$

A hypothesis space that is large enough so that we have small errors

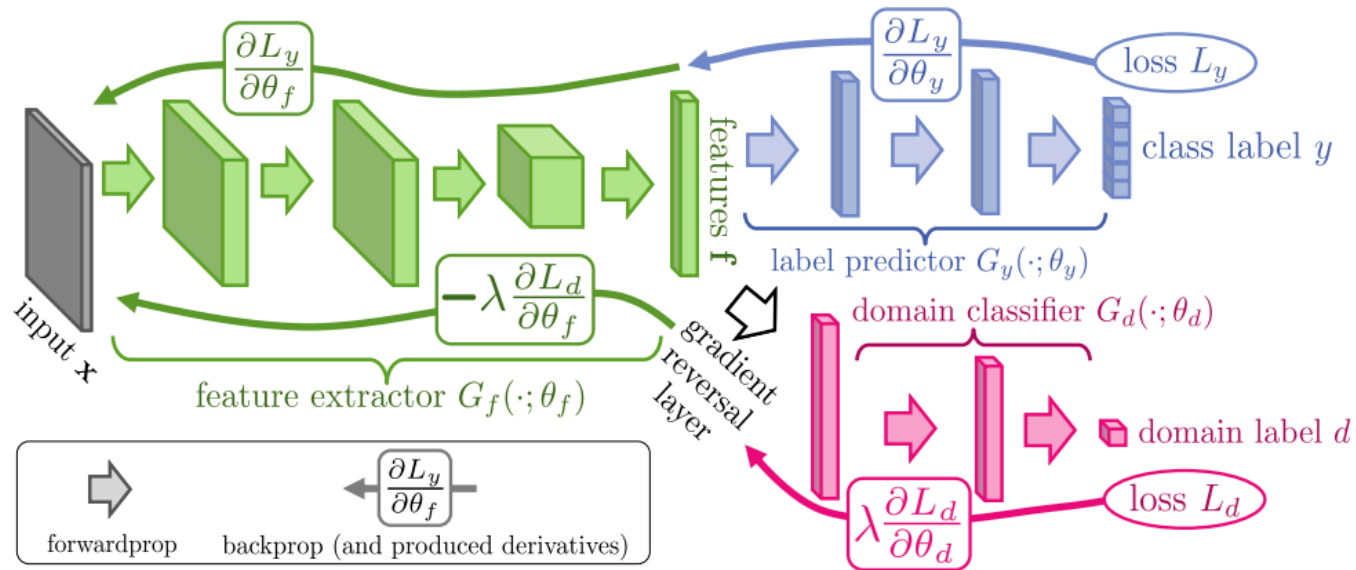




Domain Adversarial Neural Network

$$\epsilon_T(h) \leq \epsilon_S(h) + \frac{1}{2} \hat{d}_{\mathcal{H}\Delta\mathcal{H}}(\mathcal{U}_S, \mathcal{U}_T) + 4\sqrt{\frac{2d \log(2m') + \log(\frac{2}{\delta})}{m'}} + \lambda.$$

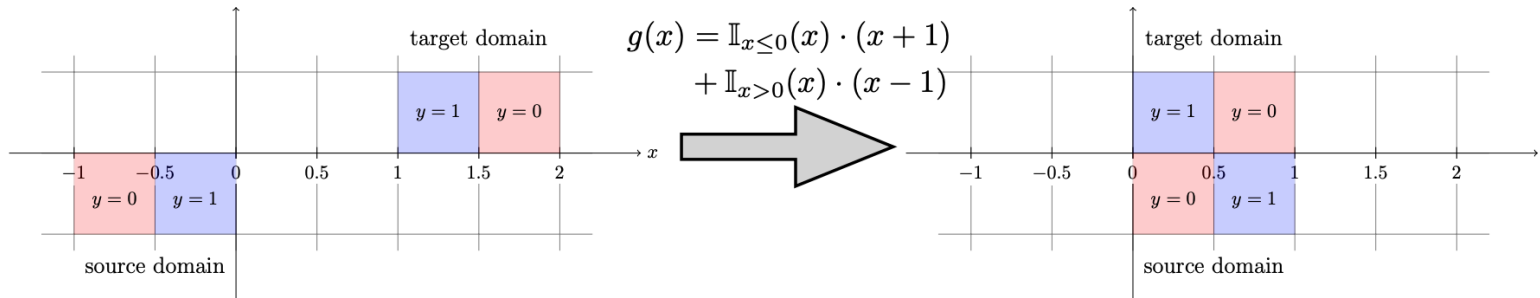
- Find a classifier that
 - has small error on the source distribution
 - unable to differentiate source and target distributions
 - (Ganin et al 2016)





Invariance regularization is not panacea

- Invariant representation and small source risk are not sufficient
 - (Zhao et al, 2019)



- Labelling function also matters

$$\varepsilon_T(h) \leq \varepsilon_S(h) + d_{\tilde{\mathcal{H}}}(\mathcal{D}_S, \mathcal{D}_T) + \min\{\mathbb{E}_{\mathcal{D}_S}[|f_S - f_T|], \mathbb{E}_{\mathcal{D}_T}[|f_S - f_T|]\}$$

Distance between labelling functions





Domain Adaptation Method Highlights

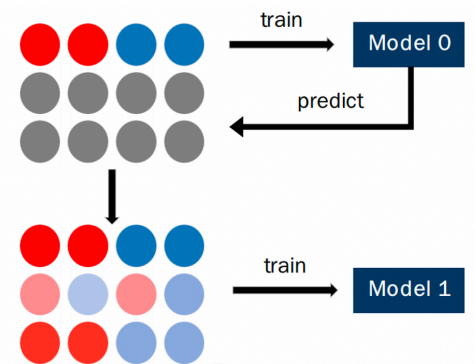
- ❑ In the deep learning era:
 - ❑ Essentially, to design an inductive bias that learns an invariance representation between source and target distributions
 - ❑ How to force the representations to be invariant?
 - ❑ Through a distance metric
 - ❑ e.g., Maximum Mean Discrepancy (MMD) (Rozantsev et al. 2016)
 - ❑ Through an adversarial classifier
 - ❑ e.g., Domain Adversarial Neural Network (DANN) (Ganin et al. 2016)
 - ❑ Through reconstruction
 - ❑ e.g., Deep Reconstruction Classification Network (DRCN) (Ghifary et al. 2016)



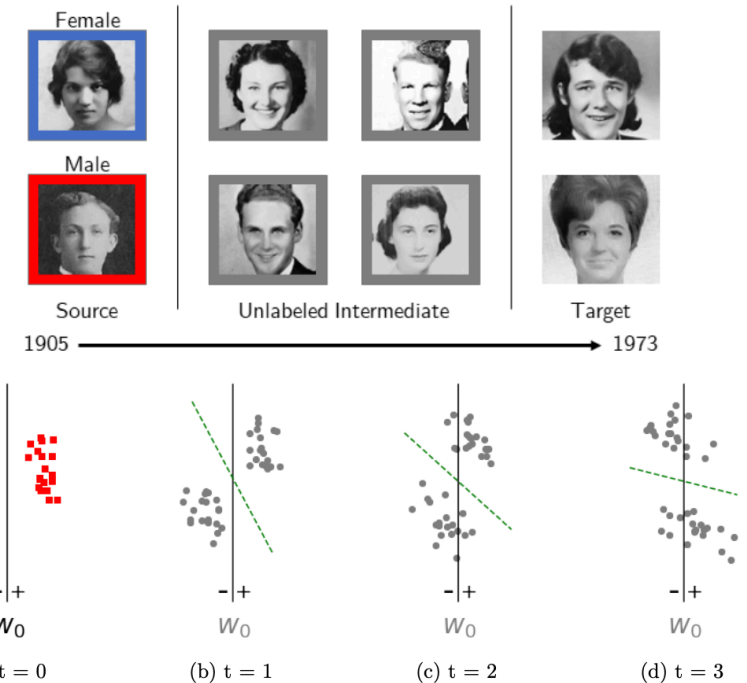


Domain Adaptation Method Highlights

- With the power of samples
 - Self-Training for Gradual Domain Adaptation
 - (Kumar et al. 2020)



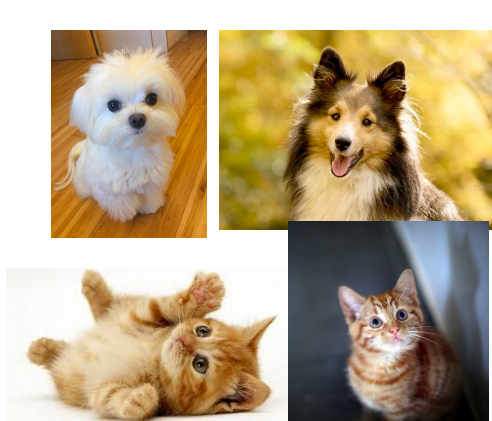
- Practical insights
 - There must be an incentive for the model to update itself
 - Regularization is necessary
 - Label-sharpening (instead of probabilistic labels) is necessary





Domain Generalization

- Are models trained for domain adaptation good enough for a general real-world deployment?
 - Probably not. --- there might be other distributions that are not considered as target distributions during training.
- Domain Generalization
 - Train with samples from different domains, and test it with a new distribution



During Training



During Testing





Domain Generalization Methods Highlights

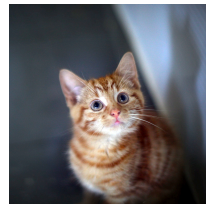
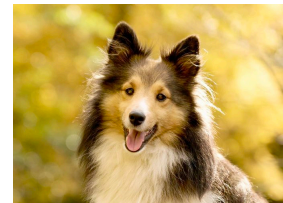
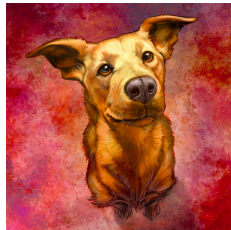
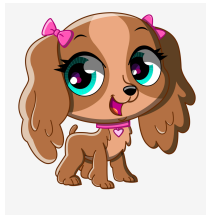
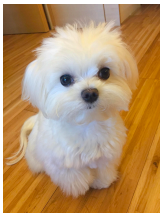
- ❑ Taking advantage of the domain identifications
 - ❑ Central assumption:
 - ❑ The model that can generalize similarly and well across different training distributions will be able to generalize well to an arbitrary target distribution
 - ❑ Method Development
 - ❑ Forcing invariance across different distributions
 - ❑ e.g., select-additive learning (Wang *et al.*, 2017)
 - ❑ Ensemble of classifiers (one for each domain)
 - ❑ e.g., best-source forward (Mancini *et al.*, 2018)
 - ❑ Meta-learning
 - ❑ e.g., iteratively split training domains to virtual training and testing domains (Li et al., 2018)



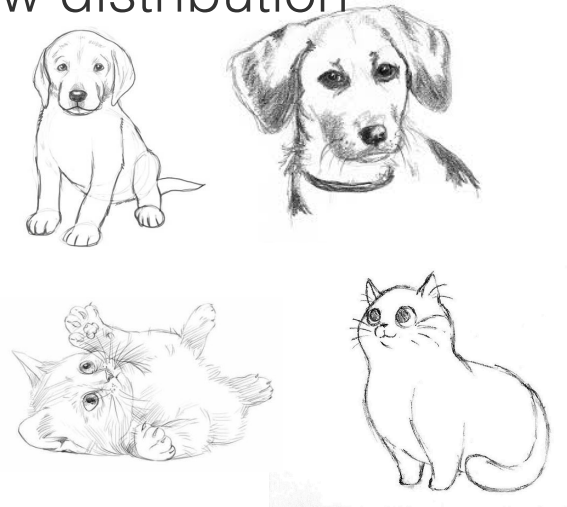


Beyond Domain Generalization

- Are models trained for domain generalization good enough for a general real-world deployment?
 - Probably not. – the partitions of domains may not always be available in the real world.
- Beyond Domain Generalization
 - Train with samples from some domains, and test it with a new distribution



During Training



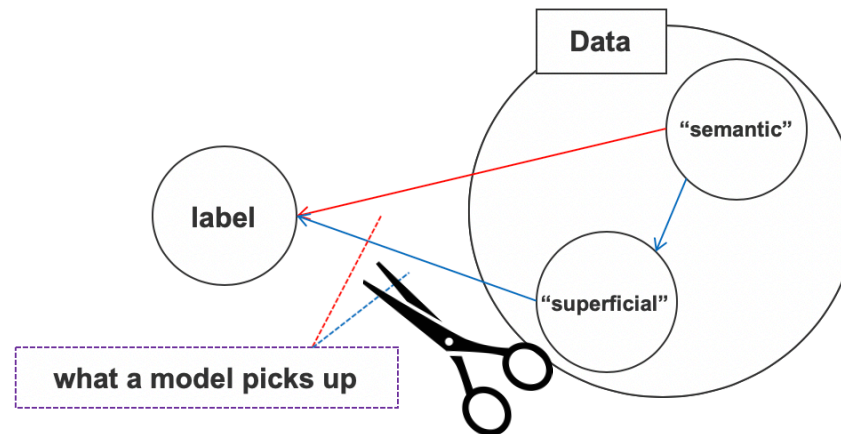
During Testing





Beyond Domain Generalization

- Now, we probably have a problem that is real enough
 - But how to solve it then?



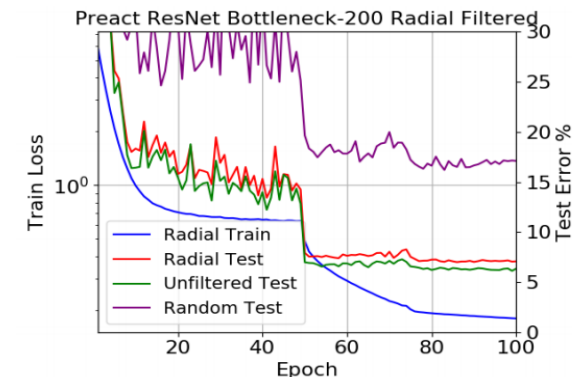
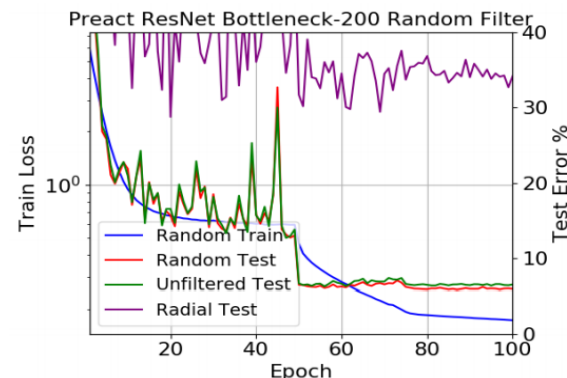
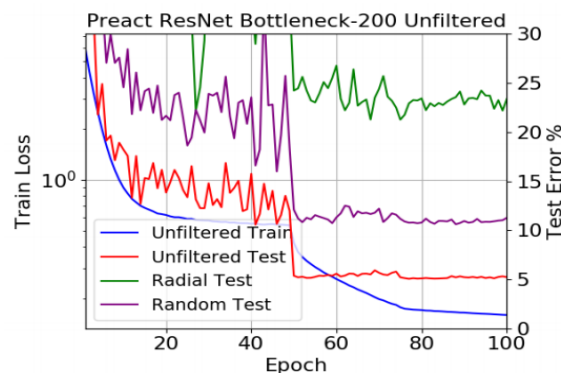
- Find a hypothesis space that pick less superficial signals
 - Case Studies:
 - Neural GLCM (Wang et al. 2019a)
 - Patch-wise Adversarial Regularization (Wang et al. 2019b)





Learning Robust Representations by Projecting Superficial Statistics

- The challenge
 - Neural networks learn textural signals
 - (Jo and Bengio 2017)
 - And many examples we have seen





A Superficial Statistics Learner

- Existing computer vision techniques
 - SURF (Bay et al., 2006)
 - LBP (He & Wang, 1990)
 - GLCM (Haralick et al., 1973)
- Semantic vs. Textural Experiments
 - Digits (MNIST, SVHN, MNIST-M, USPS)
 - Digit classification vs. Domain classification
 - Rotated MNIST
 - Digit classification vs. Rotation classification
 - FFT Kernelled MNIST
 - Digit classification vs. Kernel classification

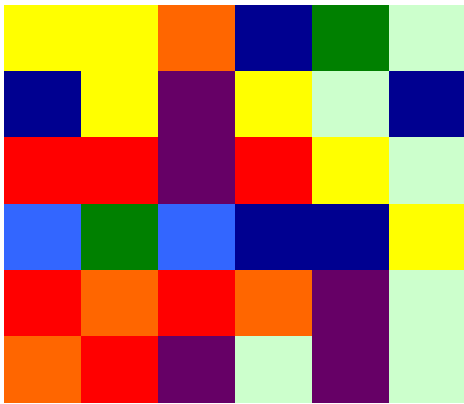
		LBP	SURF	GLCM
Digit	Semantic	0.179	0.563	0.164
	Textural	0.527	0.809	0.952
Rotated	Semantic	0.155	0.707	0.214
	Textural	0.121	0.231	0.267
FFT	Semantic	0.710	0.620	0.220
	Textural	0.550	0.200	0.490





Gray-Level Co-Occurrence Matrix

- Count the number of pixel pairs under a certain direction



Image

1	1	7	5	3	2
5	1	6	1	2	5
8	8	6	8	1	2
4	3	4	5	5	1
8	7	8	7	6	2
7	8	6	2	6	2

Pixel

	1	2	3	4	5	6	7	8
1								
2								
3								
4								
5								
6								
7								
8								

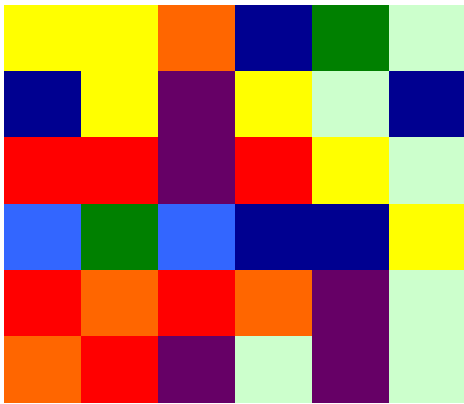
GLCM



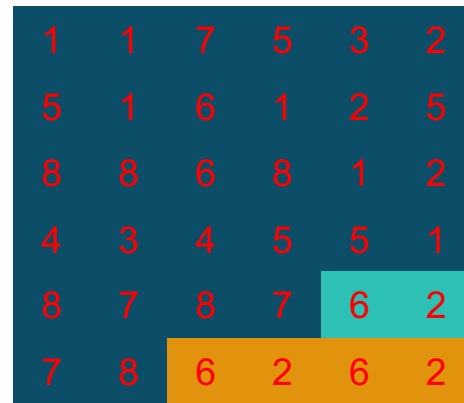


Gray-Level Co-Occurrence Matrix

- Count the number of pixel pairs under a certain direction



Image



Pixel

	1	2	3	4	5	6	7	8
1								
2								
3								
4								
5								
6		3						
7								
8								

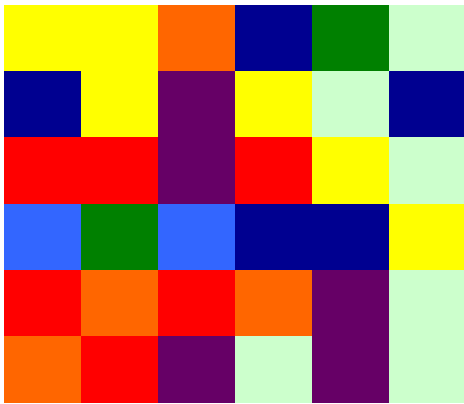
GLCM



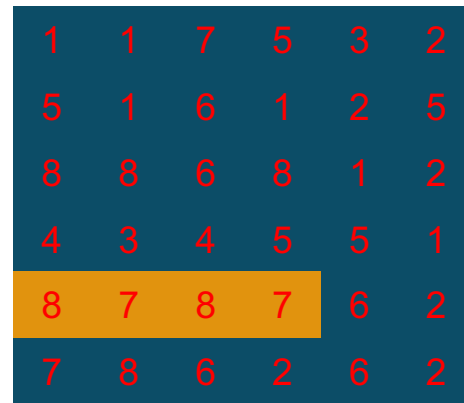


Gray-Level Co-Occurrence Matrix

- Count the number of pixel pairs under a certain direction



Image



Pixel

	1	2	3	4	5	6	7	8
1								
2								
3								
4								
5								
6		3						
7								
8							2	

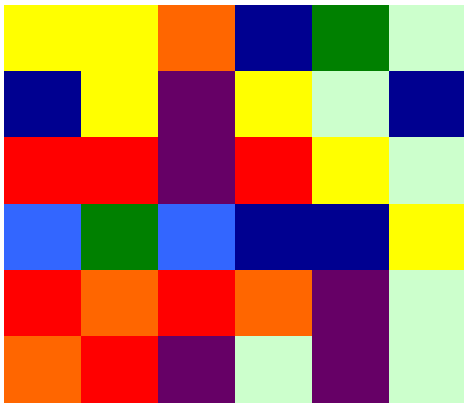
GLCM





Gray-Level Co-Occurrence Matrix

- Count the number of pixel pairs under a certain direction



Image

1	1	7	5	3	2
5	1	6	1	2	5
8	8	6	8	1	2
4	3	4	5	5	1
8	7	8	7	6	2
7	8	6	2	6	2

Pixel

	1	2	3	4	5	6	7	8
1	1	2	0	0	0	1	1	0
2	0	0	0	0	1	1	0	0
3	0	1	0	1	0	0	0	0
4	0	0	1	0	1	0	0	0
5	2	0	1	0	1	0	0	0
6	1	3	0	0	0	0	0	1
7	0	0	0	0	1	1	0	2
8	1	0	0	0	0	2	2	1

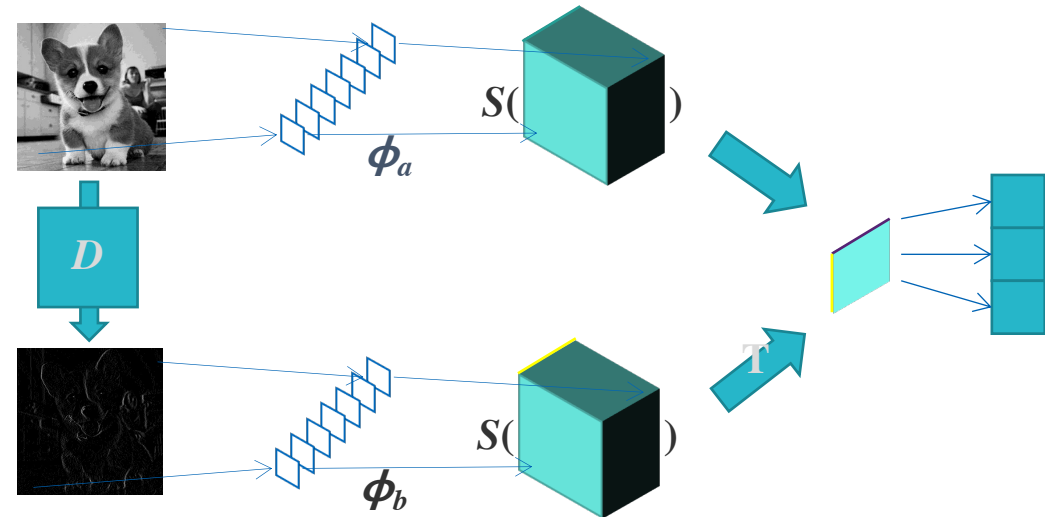
GLCM





Neural Gray-Level Co-Occurrence Matrix

- Built into a neural network
 - Enable end-to-end learning
 - Differentiate weights





Synthetic Experiments: TESTING HEX Method

- Office data set
 - Webcam (W)
 - Amazon (A)
 - DSLR (D)
- Testing with the Beyond Domain Generalization setting

Train	Test	Baseline	HEX
A+W	D	0.405±0.016	0.343±0.030
D+W	A	0.112±0.008	0.147±0.004
A+D	W	0.400±0.016	0.378±0.034

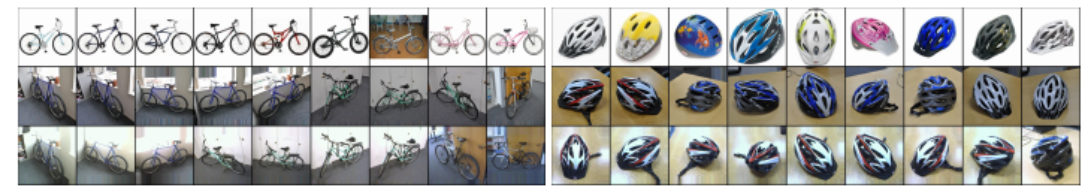




OFFICE DATA SET: A CLOSER LOOK

- Distribution similarities between D and W
- Two classifier:
 - C1: classifying object based on object and background
 - C2: classifying object based on object, ignoring background

Train	Test	Baseline (C1)	HEX (C2)
A+W	D	0.405±0.016	0.343±0.030
D+W	A	0.112±0.008	0.147±0.004
A+D	W	0.400±0.016	0.378±0.034



(a) Bike

(b) Bike Helmet



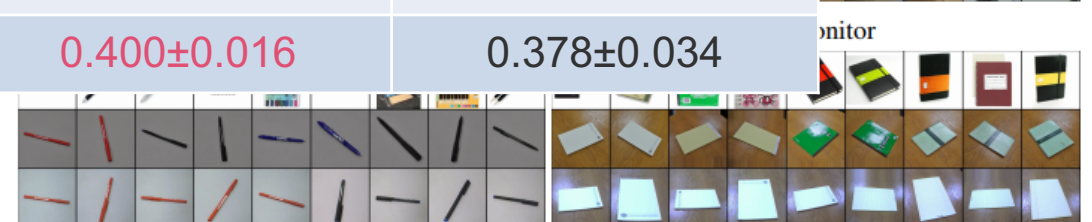
(c) Book Case

(d) Bottle



(e) Desktop Computer

(f) Laptop Computer



(k) Pen

(l) Paper Notebook



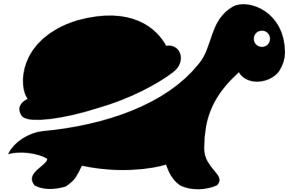


Learning Robust Presentations by Penalizing the Local prediction power

- The challenge
 - Neural networks can predict through local signals, that do not align well with the annotation of the dataset

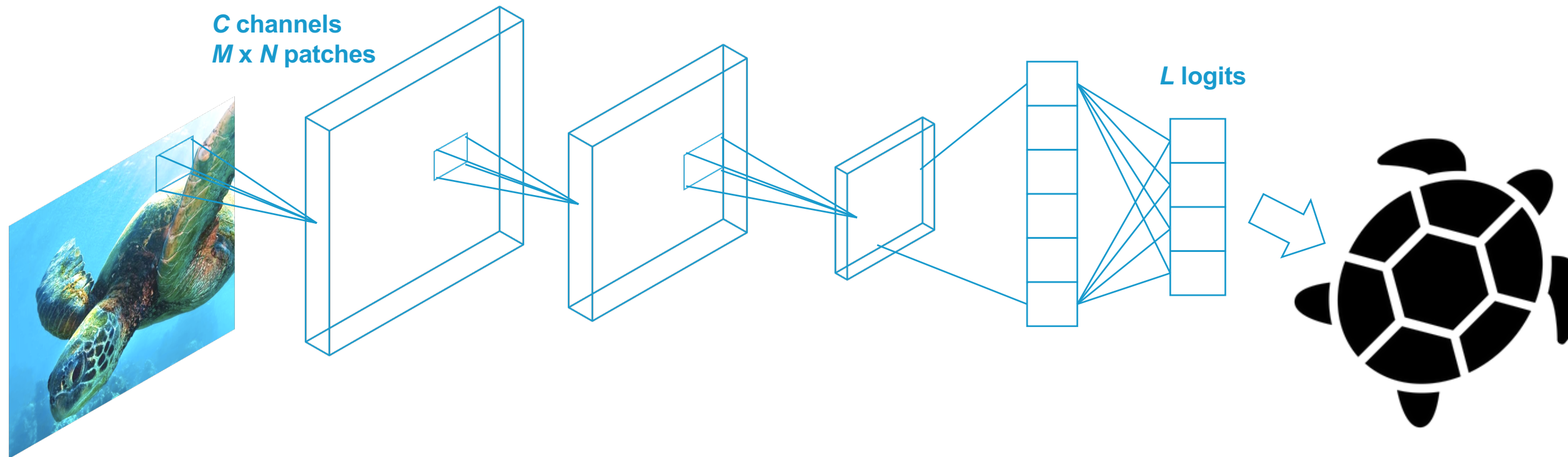


VS



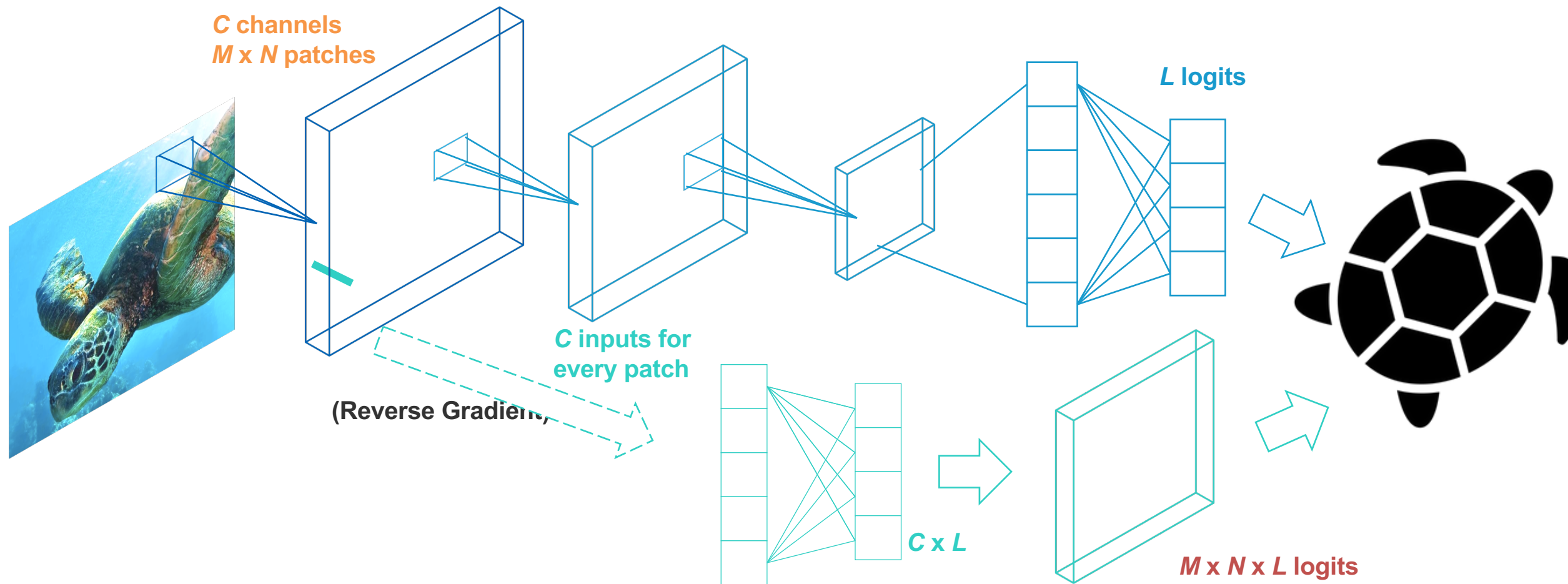


Patch-wise Adversarial Regularization



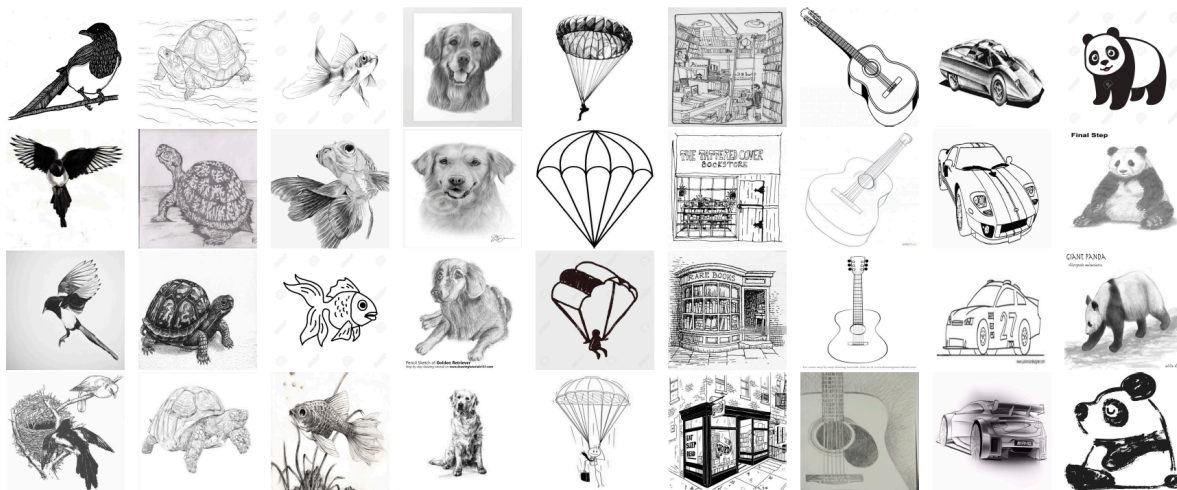


Patch-wise Adversarial Regularization





Results – ImageNet Sketch



ImageNet-Sketch Data set

- ImageNet-Sketch data set consists of 50000 images, 50 images for each of the 1000 ImageNet classes.

Results

	AlexNet-PAR		AlexNet	
	prediction	confidence	prediction	confidence
	stethoscope	0.6608	hook	0.3903
	tricycle	0.9260	safety pin	0.5143
	Afghan hound	0.8945	swab (mop)	0.7379
	red wine	0.5999	goblet	0.7427





 $+ .007 \times$  $=$ 

x $\text{sign}(\nabla_x J(\theta, x, y))$ $x + \epsilon \text{sign}(\nabla_x J(\theta, x, y))$

“panda” “nematode” “gibbon”

57.7% confidence 8.2% confidence 99.3 % confidence

Adversarial Robustness



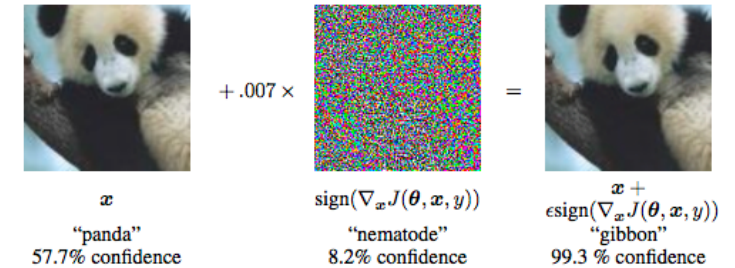


What are adversarial examples

- Recap, with the help of the most popular example
- What are adversarial examples?
 - Samples with carefully crafted patterns added to an original sample, and
 - look identical to the original image to human,
 - but predicted by a model significantly different from the original sample.
 - This sounds quite magic, but not rigorous enough...
 - With sample x , model $f(\cdot; \theta)$, the adversarial example x' is

$$x' = \arg \min_{x': f(x'; \theta) \neq f(x; \theta)} d(x, x')$$

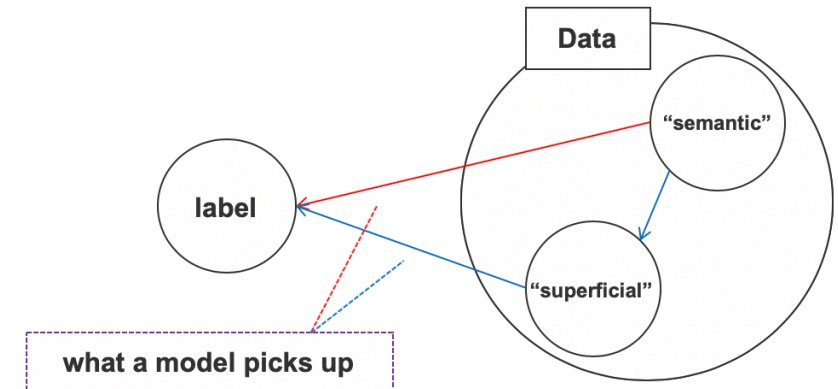
- A result of an optimization, $d(\cdot)$ is a distance
- Hopefully, this does not sound too magic anymore.
 - How magic it looks to human depends on the choice of $d(\cdot)$





What are adversarial examples

- Why are there adversarial examples?
 - Adversarial examples are direct outcomes of the fact
 - **models are capturing superficial signals**
 - (Ilyas *et al.* 2019)
 - (Wang *et al.* 2020)
- Why is adversarial robustness a popular topic
 - Hmm..., one reason might actually be it appears magic
 - The alignment between human and model may play a significant role in the real-world deployment of machine learning
- As a popular topic
 - Tons of efforts made to defend a model against adversarial examples
 - Unfortunately, even more efforts made to generate new adversarial examples...

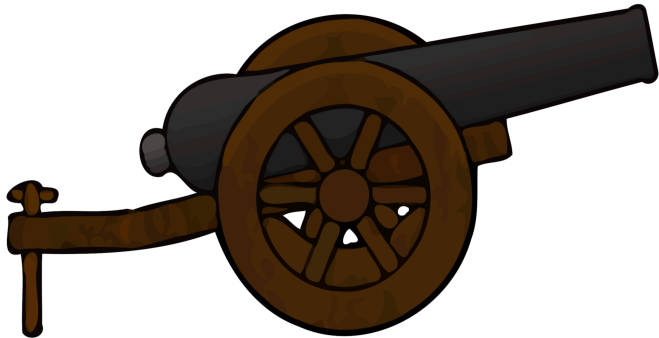




The Attack vs. Defense Arm Race Highlights

□ Attack Methods

- FGSM
 - (Goodfellow et al. 2014)
- PGD
 - (Madry et al. 2017)



□ Defense Methods

- TRADES
 - (Zhang et al. 2019)
- Adversarial Training
 - (Madry et al. 2017)

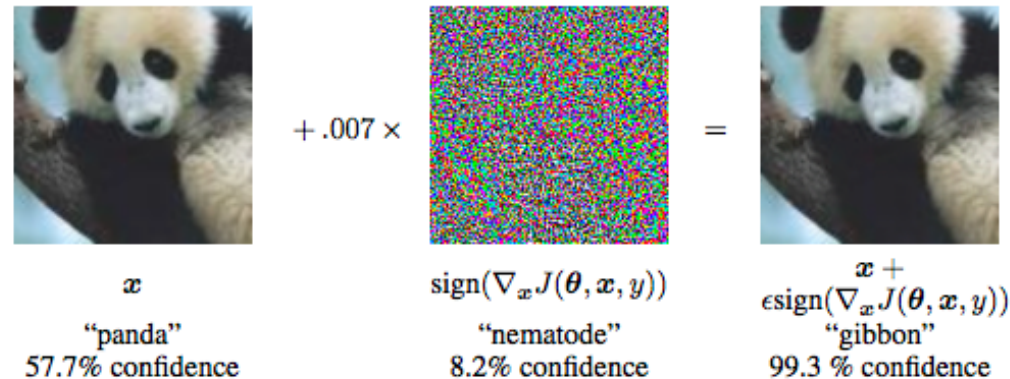




The Attack vs. Defense Arm Race Highlights

- Fast Gradient Sign Method (FGSM)
 - (Goodfellow et al. 2014)
 - Intuitively: a reverse way of training
 - Training (one epoch) is to update parameters to decrease loss, according to the gradient
 - FGSM is to update the data to increase loss, according to the sign of the gradient

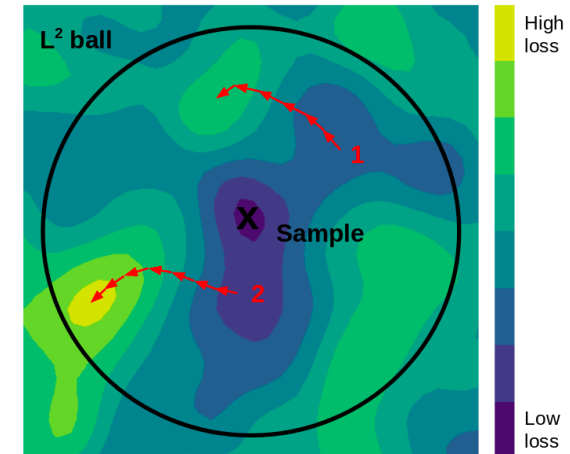
$$x' = x + \epsilon \text{sign}(\nabla_x l(x, y; \theta))$$





The Attack vs. Defense Arm Race Highlights

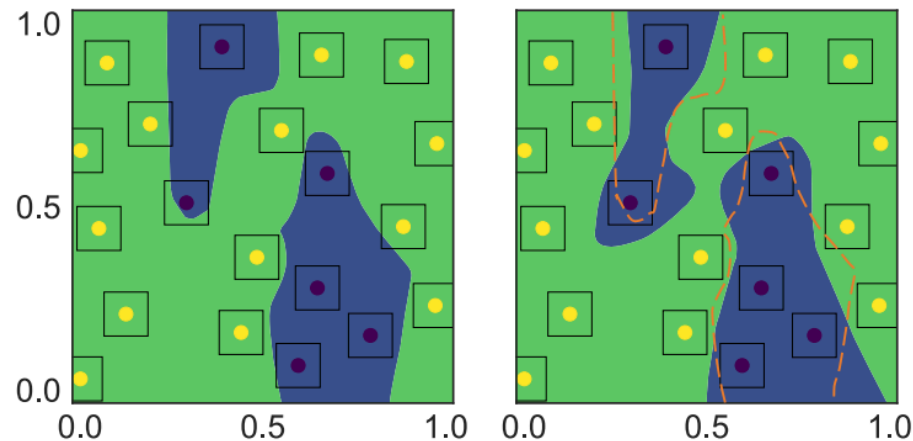
- ❑ PGD (Projected Gradient Descent) attack
 - ❑ (Madry *et al.* 2017)
 - ❑ Fun fact, it's previously invented under the name Basic Iterative Method (BIM)
 - ❑ Algorithm: Performing FGSM multiple times, with smaller step size.
 - ❑ Start with a random perturbation within the l_p norm ball
 - ❑ Perform FGSM: $x' = x + \epsilon \text{sign}(\nabla_x l(x, y; \theta))$
 - ❑ Project back to the l_p norm ball
 - ❑ Repeat multiple iterations
- ❑ Probably the most powerful attack method nowadays (l_p norm distance)





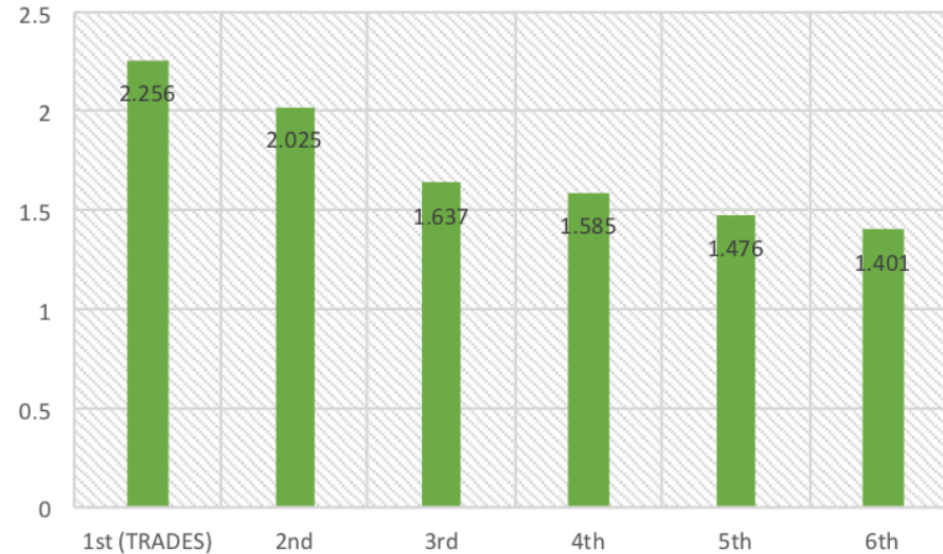
The Attack vs. Defense Arm Race Highlights

- TRADES Defense
 - (Zhang *et al.* 2019)
 - Take advantage of the worst-case example
 - To identify the worst-case example
 - Apply attack during training to identify x'
 - Regularize the distance of embedding between x and x'
 - KL divergence regularization over softmax





Competition: NeurIPS 2018 Adversarial Vision Challenge



The methodology is the foundation of our entry to the NeurIPS 2018 Adversarial Vision Challenge in which we won the 1st place out of ~2,000 submissions, surpassing the runner-up approach by 11.41% in terms of mean l_2 perturbation distance





The Attack vs. Defense Arm Race Highlights

- Adversarial Training as a Defense
 - (Madry et al. 2017)
 - Summarize in one sentence:
 - augment the training data with generated adversarial examples during training
 - The most popular defense method
 - When integrated with PGD
 - Impressive empirical performance and simplicity

As we see in next slide.

The community is making it easier:

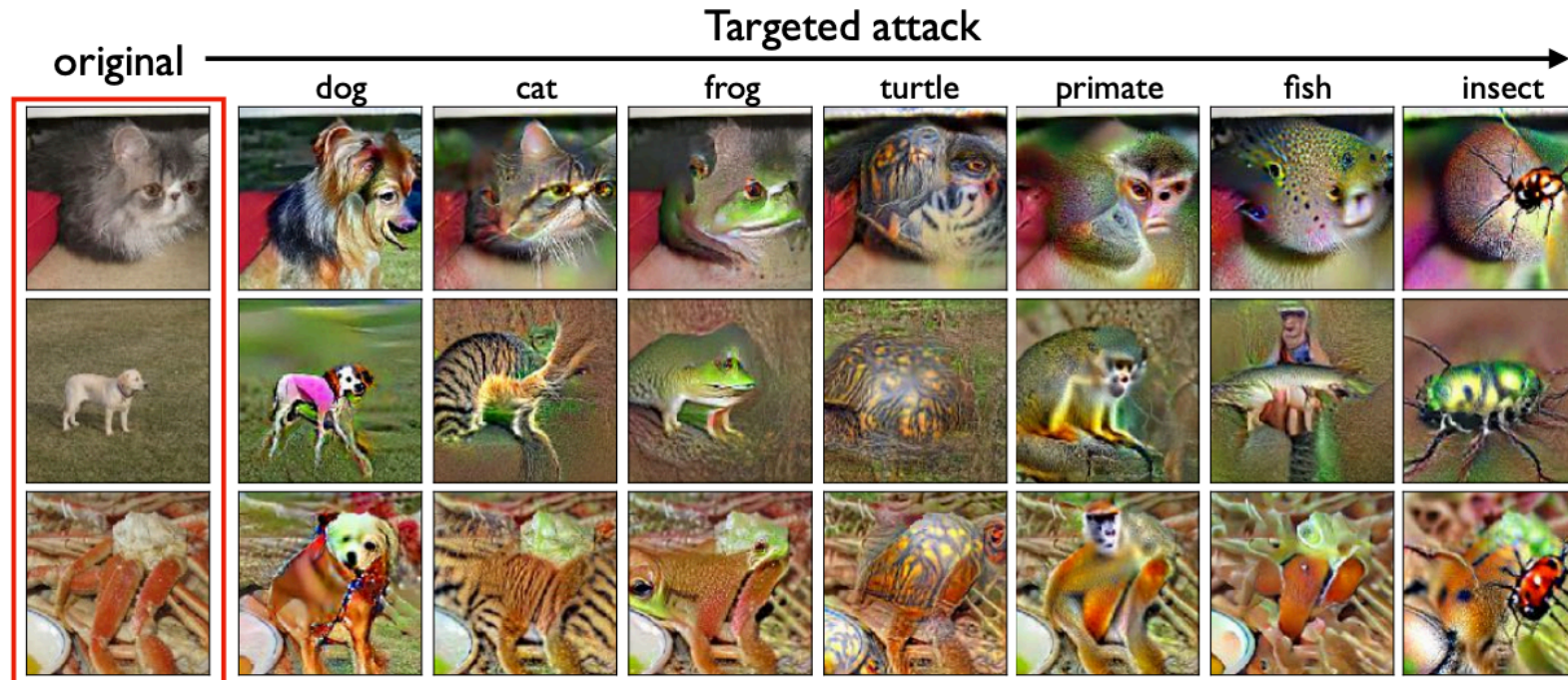
- A faster (than PGD) way to generate the adversarial examples (that are equally powerful to the ones generated by PGD)
 - Adversarial training for free. Shafahi *et al.* 2019
 - Fast is better than free. Wong *et al.* 2020





Perceptually Aligned Representations from Adversarial Training w. PGD

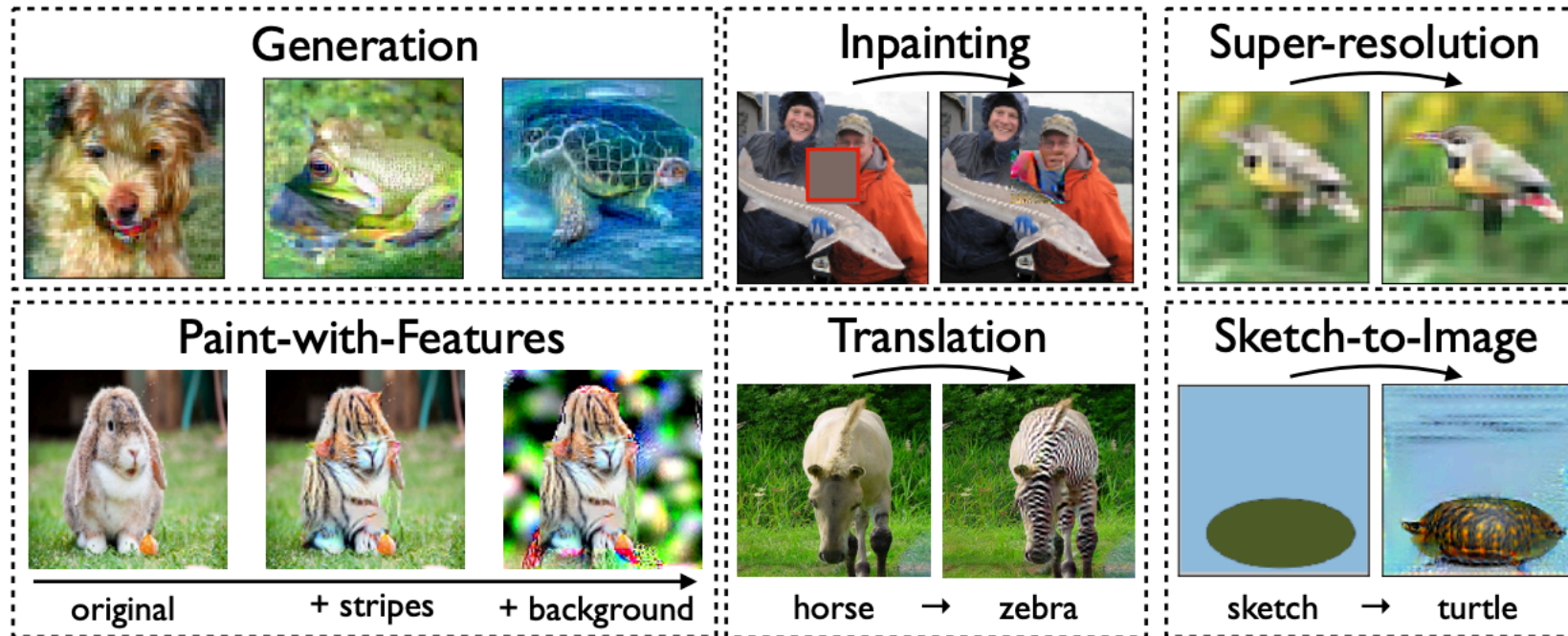
- With PGD + adversarial training, adversarial examples are not that magical any more
 - (Santurkar et al. 2019)





Perceptually Aligned Representations from Adversarial Training w. PGD

- With PGD + adversarial training, the same model may fulfill multiple tasks
 - (Santurkar et al. 2019)





The Attack vs. Defense Arm Race

- ❑ With the impressive performance of PGD + adversarial training, can we conclude the development of defense methods?
 - ❑ Maybe not: It's simple, not not simple enough
 - ❑ Definitely not: there might be other attack methods can penetrate the defended model
 - ❑ So... is this race endless?
 - ❑ Fortunately, the community moves to provably robust models.





Certified Robust Models

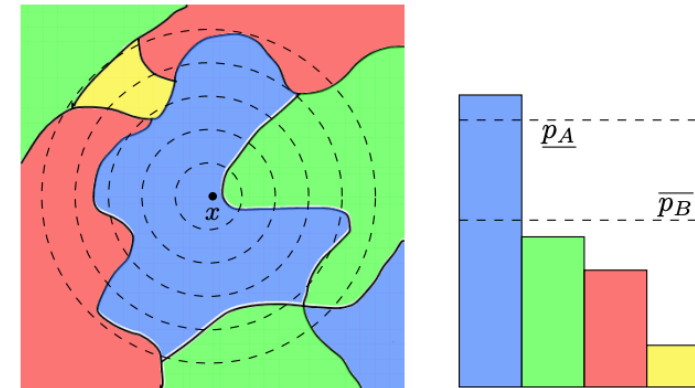
- Certified Robustness through Randomized Smoothing

- (Cohen et al. 2019)
- Randomized smoothing method

$$g(x) = \arg \max_{c \in \mathcal{Y}} \mathbb{P}(f(x + \varepsilon) = c)$$

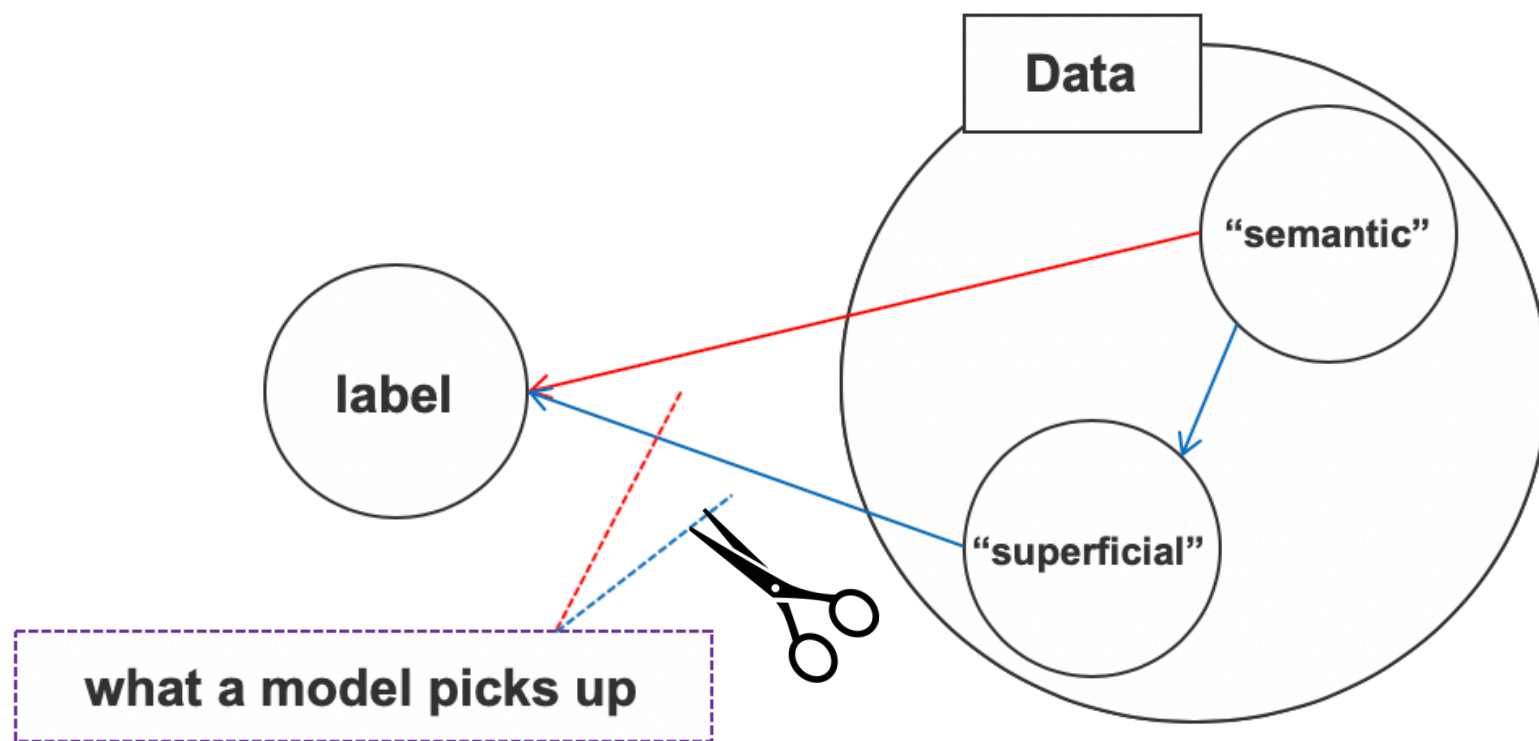
where $\varepsilon \sim \mathcal{N}(0, \sigma^2 I)$

- **Certified Robustness**
 - Over l_2 norm distance





Looking into the Future





A Brief Overview of Trustworthy Machine Learning

- ❑ New Challenges of Modern Machine Learning
 - ❑ Empirical Observations
 - ❑ Trade-off between Accuracy and Robustness
- ❑ Cross-domain Robust Models
 - ❑ Generalization Analysis of Domain Adaptation
 - ❑ Method Overview – It's mostly about Invariance
 - ❑ Domain Generalization and Beyond
- ❑ Adversarial Robust Models
 - ❑ The Attack vs. Defense Arm Race Highlights
 - ❑ Adversarial Training and Its Recent Developments
 - ❑ Certified Robustness and Generalization Analysis





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